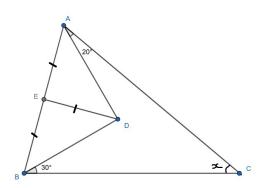
M. Prakash Institute Time: 2 Hours

IX Entrance Exam 20 April 2025

- 1. Consider the consecutive prime numbers between 1 and 100. Suppose there are m pairs of adjacent primes with a difference of 6. What is the value of 2m?
- 2. Nine friends went to a party. All the boys drank only coffee, and all the girls drank only tea. The price of one cup of coffee (in rupees) is 2 less than the number of girls. The price of one cup of tea (in rupees) is 2 less than the number of boys. The total money spent by the boys and the girls is in the ratio 5:6. Find the cost of 10 cups of coffee.
- 3. If m and n are solutions of the quadratic equation $8x^2 25x + 18 = 0$, find the value of 8mn.
- 4. In the following diagram (not to scale), \underline{D} is in the interior of $\triangle ABC$. E is on \overline{AB} such that AE = BE = DE. If $m\angle DAC = 20^{\circ}$, $m\angle DBC = 30^{\circ}$, and $m\angle ACB = x$, find x.

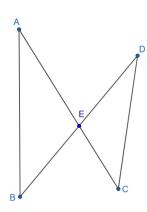


5.
$$P = \left(\frac{\sqrt[3]{64}}{\sqrt[3]{32}} \times \sqrt[4]{16}\right)^3$$
. Find P .

- 6. 10% of 20% of 40% of 50% of 80% of 15000 is?
- 7. The average age of a family of 4 is 22 years and 6 months. The son is 2 years older than his sister. The father is 4 years older than his wife. What is the average age of the mother and son?

8.
$$\left[\frac{8}{7} + \frac{7}{8}\right]^2 - \left[\frac{8}{7} - \frac{7}{8}\right]^2 = x$$
, find x^2 .

9. In the following diagram (not to scale), segments \overline{AC} and \overline{BD} intersect at E. If $m\angle BAE = m\angle ECD + 20^{\circ}$ and $m\angle CDE = 60^{\circ}$, find $m\angle ABE$.

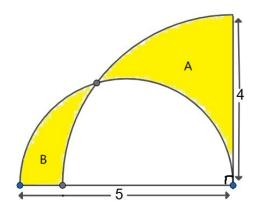


10. If y is a natural number that satisfies the equation below, then find y^2 :

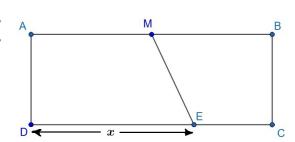
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$$1 + \frac{y+3}{y-2} = \frac{3y-3}{6-y}$$

- 11. If a sum doubles in 80 months at simple interest, how many years will it take for the sum to become four times its original amount?
- 12. In a triangle, the largest angle is twice the measure of the second largest angle. One third of the largest angle is 10° more than the difference between the other two angles. Find one third of the largest angle.
- 13. If a + b = 16, $a^2 + b^2 = 130$, find the sum of the digits of $a^3 + b^3$.
- 14. A semicircle and a quarter circle are shown in the figure. The radius of the quarter circle is 4 and the diameter of the semicircle is 5. The shaded area A is inside the quarter circle but outside the semicircle. The shaded area B is inside the semicircle but outside the quarter circle. If $A B = \frac{a\pi}{b}$, find a + b.



- 15. Let a, b, and c be numbers such that $ac = \frac{4}{b}$ and b(a+c) + ac = 32. Find the value of $\frac{3}{a} + \frac{3}{b} + \frac{3}{c}$.
- 16. A two-digit number is four times the sum of its digits and twice the product of the digits. Find the number.
- 17. In rectangle $\Box ABCD$, AB = 24, BC = 18. M is the midpoint of \overline{AB} . E is on \overline{DC} at a distance x from D. Find x such that the area of $\Box AMED$ is twice the area of $\Box BMEC$.



- 18. $\frac{\sqrt{5} + \sqrt{3}}{\sqrt{5} \sqrt{3}} = a b\sqrt{15}$. Find 3(a b).
- 19. Find natural number x such that: $\sqrt{x^2 + x + 17} = 17$
- $20.\$ If 22 weavers weave 990 shawls in 15 days, how many weavers can weave 630 shawls in 21 days?

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